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DMI-ST. EUGENE UNIVERSITY

ZAMBIA

DEGREE EXAMINATION – JUNE 2023

Semester: I

800MA102

MATHEMATICS - I

Time: 3:00 Hours

Max. Marks: 100

Answer any FIVE Questions(5 x 20 = 100 Marks)

- Describe the various types of sets . (10 Marks)
 - If Set $A = \{1,2,3,4\}$, $B = \{2,4,6,8\}$ and $C = \{3,4,5,6\}$ are subsets of the universal set $U = \{1,2,3,4,5,6,7,8,9,10\}$ list the elements of the set (i) $A \cup (B \cap C)$ (ii) $A \cap B \cap C$ (5 Marks)
 - If $A = \{3,5,7,9,11\}$, $B = \{7,9,11,13\}$ and $C = \{11,13,15\}$ Find (i) $(A \cap B) \cap (B \cup C)$
(ii) $A \cup B \cup C$ (5 Marks)
- Prove the identity $\frac{\tan x + \sec x}{\sec x \left(1 + \frac{\tan x}{\sec x}\right)} = 1$ (10 Marks)
 - Solve the equation $3 \tan^3 x = \tan x$ for $0 \leq x < 2\pi$. (5 Marks)
 - Convert $40^\circ 20'$ into radian measure. (5 Marks)
- Find the derivative of the following function: $f(x) = \sin x \cos x$ (10 Marks)
 - Find the derivative of $f(x) = \frac{1}{x}$. (5 Marks)
 - Find the limit $\lim_{x \rightarrow 1} \left[\frac{x-2}{x^2-x} - \frac{1}{x^3-3x+2x} \right]$ (5 Marks)
- Find the distance between the points $P(1, -3, 4)$ and $Q(-4, 1, 2)$. (10 Marks)
 - Find the distance between parallel lines
(i) $15x + 8y - 34 = 0$ and $15x + 8y + 31 = 0$
(ii) $l(x + y) + p = 0$ and $l(x + y) - r = 0$ (10 Marks)
- Two coins are tossed once. find the sample space. (5 Marks)

b) Find the mean deviation about the median for the following data

3,9,5,3,12,10,18,4,7,19,21

(5 Marks)

c) Find the mean and variance of :

(10 Marks)

x:	6	10	14	18	24	28	30
f:	2	4	7	12	8	4	3

6. a) The weight (in kg) of 13 students in a class are 42.5, 47.5, 48.6, 50.5, 49, 46.2, 49.8, 45.8, 43.2, 48, 44.7, 46.9, 42.4. Find the range and coefficient of range. **(10 Marks)**

b) One card is drawn from a well shuffled deck of 52 cards. Find the probability of getting a diamond card? **(5 Marks)**

c) Define a sample space and range **(5 Marks)**

7. a) line through the points, $(-2,6)$ and $(4,8)$ is perpendicular to the line through the points $(8,12)$ and $(x,24)$ find the value of x . **(10 Marks)**

b) Find the ratio in which the YZ-plane divides the line segment formed by joining the points $(-2, 4, 7)$ and $(3, -5, 8)$. **(10 Marks)**